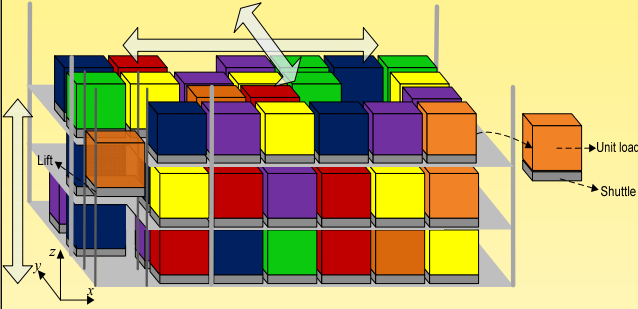
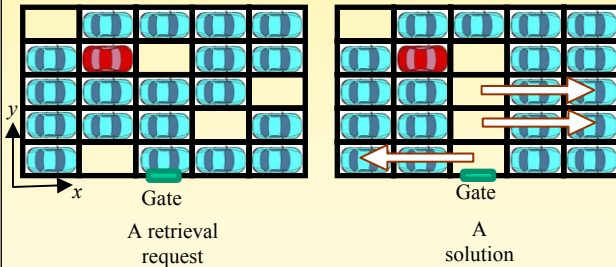


Introduction

• Puzzle-based compact storage system



• Work mechanism



Objective

• **Research question:** How to optimize dimensions of a puzzle-based storage system, leading to the minimum response time in a random storage policy.

• Assumptions:

1. The system capacity is a known positive constant.
2. A random storage policy is assumed.

• **Theorem.** The minimum retrieval time of a random unit load stored at location (X, Y, Z) , can be estimated by the following equation:

$$RT(X, Y, Z) = \max\{X+Y, Z\} + Z, \quad (1)$$

if the utilization of the system does not exceed $(V' - \max\{L, W\})/V'$, where V' , L , and W represent the capacity of the system in number of storage locations, the number of columns in each level, and the number of rows in each level, respectively.

A random retrieval location can be denoted by (X, Y, Z) where X , Y and Z refer to coordinates in x-, y- and z-directions respectively.

Mathematical model

$$\text{Min } ERT, \quad (2)$$

subject to:

$$l \times w \times h = V, \quad (3)$$

decision variables: $l > 0, w > 0, h > 0,$

where l , w , and h (length, width, height of the system) are the decision variables. All the dimensions are expressed in time units. V represents the volume of the system in cubic time unit. Constraint (3) makes sure the given capacity is achieved.

Methodology

• The model is non-linear and mixed integer; however, we can optimally solve it by splitting it into several solvable sub-models

• In order to solve the model we have to derive ERT in Equation (2). The expected retrieval time for any puzzle-based system with a given capacity can be calculated as follows:

$$ERT = \int_{t=0}^{\max\{w+l, h\}+h} f(t) dt \quad (4)$$

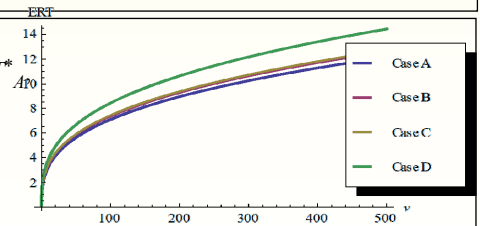
where, t represents the retrieval time for any retrieval location. $f(t)$ represents the probability density function of retrieval time t .

• Calculation of ERT can be done into four different complementary cases, each referring to a specific configuration of the system:

Case A: $h \leq w$, **case B:** $w < h \leq l$, **case C:** $l < h \leq l+w$, **case D:** $l+w < h$.

Findings and conclusions

The following figure give ERT^* , ERT_B^* , ERT_C^* and ERT_D^* as a function of V .



The solution of case A ($h \leq w$) gives the minimal ERT for the Model.

$$h^*(V) = 0.874461V^{1/3} \quad (5)$$

$$l^*(V) = w^*(V) = 1.069374V^{1/3} \quad (6)$$